

# First Six Weeks Math Standards Sequence Grade Alg 1

Domain	Cluster	Standard	Dates
Real Number System	Use properties of rational and irrational numbers	3. Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational.	1 <sup>st</sup> six weeks
Quantities	Reason quantitatively and use units to solve problems	1. Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.	1 <sup>st</sup> six weeks
		2. Define appropriate quantities for the purpose of descriptive modeling.	1 <sup>st</sup> six weeks
		3. Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.	1 <sup>st</sup> six weeks
Seeing Structure in Expressions	Interpret the structure of expressions	1. Interpret expressions that represent a quantity in terms of its context. ★ a. Interpret parts of an expression, such as terms, factors, and coefficients. b. Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret $P(1+r)^n$ as the product of $P$ and a factor not depending on $P$ .	1 <sup>st</sup> six weeks
Creating Equations	Create equations that describe numbers or relationships	1. Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.	2 <sup>nd</sup> six weeks
		2. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.	2 <sup>nd</sup> six weeks
		3. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.	2 <sup>nd</sup> six weeks
		4. Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law $V = IR$ to highlight resistance $R$ .	2 <sup>nd</sup> six weeks
Reasoning with equations and inequalities	Understand solving equations as a process of reasoning and explain the reasoning	1. Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.	2 <sup>nd</sup> six weeks
	Solve equations and inequalities in one variable	3. Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.	2 <sup>nd</sup> six weeks
Interpreting functions	Understand the concept of a function and use function notation	1. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If $f$ is a function and $x$ is an element of its domain, then $f(x)$ denotes the output of $f$ corresponding to the input $x$ . The graph of $f$ is the graph of the equation $y = f(x)$ .	2 <sup>nd</sup> six weeks

		<ol style="list-style-type: none"> <li>2. Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.</li> <li>3. Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. For example, the Fibonacci sequence is defined recursively by <math>f(0) = f(1) = 1</math>, <math>f(n+1) = f(n) + f(n-1)</math> for <math>n \geq 1</math></li> </ol>	
	Interpret functions that arise in applications in terms of the context	<ol style="list-style-type: none"> <li>4. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity. ★</li> <li>5. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function <math>h(n)</math> gives the number of person-hours it takes to assemble <math>n</math> engines in a factory, then the positive integers would be an appropriate domain for the function. ★</li> <li>6. Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. ★</li> </ol>	2 <sup>nd</sup> six weeks
Building Functions	Build a function that models a relationship between two quantities	<ol style="list-style-type: none"> <li>1. Write a function that describes a relationship between two quantities. ★ <ol style="list-style-type: none"> <li>a. Determine an explicit expression, a recursive process, or steps for calculation from a context.</li> </ol> </li> </ol>	2 <sup>nd</sup> six weeks
Linear, Quadratic, Exponential Models	Construct and compare linear, quadratic, and exponential models and solve problems.	<ol style="list-style-type: none"> <li>1. Distinguish between situations that can be modeled with <b>linear</b> functions and with exponential functions. <ol style="list-style-type: none"> <li>a. Prove that <b>linear</b> functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.</li> <li>b. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.</li> <li>c. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.</li> </ol> </li> <li>2. Construct <b>linear</b> and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).</li> <li>3. Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing <b>linearly</b>, quadratically, or (more generally) as a polynomial function.</li> <li>5. Interpret the parameters in a <b>linear</b> or exponential function in terms of a context. **Just linear equations</li> </ol>	2 <sup>nd</sup> six weeks
Interpreting categorical and	Interpret linear	<ol style="list-style-type: none"> <li>7. Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.</li> </ol>	2 <sup>nd</sup> six weeks

quantitative data			
Reasoning with equations and inequalities	Solve systems of equations	<p>5. Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.</p> <p>6. Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.</p>	3 <sup>rd</sup> six weeks
	Represent and solve equations and inequalities graphically	<p>10. Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line).</p> <p>11. Explain why the x-coordinates of the points where the graphs of the equations <math>y = f(x)</math> and <math>y = g(x)</math> intersect are the solutions of the equation <math>f(x) = g(x)</math>; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where <math>f(x)</math> and/or <math>g(x)</math> are linear, polynomial, rational, absolute value, exponential, and logarithmic functions. ★</p> <p>12. Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.</p>	3 <sup>rd</sup> six weeks
Seeing structures in expressions	Interpret the structure of expressions	<p>2. Use the structure of an expression to identify ways to rewrite it. For example, see <math>x^4 - y^4</math> as <math>(x^2)^2 - (y^2)^2</math>, thus recognizing it as a difference of squares that can be factored as <math>(x^2 - y^2)(x^2 + y^2)</math>.</p>	4 <sup>th</sup> six weeks
	Write expressions in equivalent forms to solve problems	<p>3. Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. ★</p> <p>a. Factor a quadratic expression to reveal the zeros of the function it defines.</p> <p>c. Use the properties of exponents to transform expressions for exponential functions. For example the expression <math>1.15t</math> can be rewritten as <math>(1.15^{1/12})^{12t} \approx 1.012^{12t}</math> to reveal the approximate equivalent monthly interest rate if the annual rate is 15%.</p>	4 <sup>th</sup> six weeks
Arithmetic with Polynomials and Rational Expressions	Perform arithmetic operations on polynomials	<p>1. Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.</p>	4 <sup>th</sup> six weeks
	Understand the relationship between zeros and factors of polynomials	<p>3. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.</p>	4 <sup>th</sup> six weeks

Seeing structure in Expressions	Write expressions in equivalent forms to solve problems	3b. Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines.	5 <sup>th</sup> six weeks
Reasoning with Equations and inequalities	Solve equations and inequalities in one variable	4. Solve quadratic equations in one variable. a. Use the method of completing the square to transform any quadratic equation in $x$ into an equation of the form $(x - p)^2 = q$ that has the same solutions. Derive the quadratic formula from this form. b. Solve quadratic equations by inspection (e.g., for $x^2 = 49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm bi$ for real numbers $a$ and $b$ .	5 <sup>th</sup> six weeks
Interpreting Functions	Analyze functions using different presentations	8. Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. a. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. 9. Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.	5 <sup>th</sup> six weeks
Building Functions	Build new functions from existing functions	3. Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$ , $k f(x)$ , $f(kx)$ , and $f(x + k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.	5 <sup>th</sup> six weeks
Linear, Quadratic, and exponential models	Construct and compare linear, quadratic, and exponential models and solve problems	1. Distinguish between situations that can be modeled with linear functions and with exponential functions. a. Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals. b. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another. c. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another. 2. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table). 3. Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function. 5. Interpret the parameters in a linear or exponential function in terms of a context.	5 <sup>th</sup> six weeks